The Climate Bits of Climate

$$\mathbf{XCLIM}_{(t,l,h)} = \mathbf{D}_{t,l,h} + \mathbf{S}_{t,l,h} + \mathbf{T}_{t,l,h} + \mathbf{M}_{t,l,h}$$

XCLIM = a climate element at time t, location I and height h

D = diurnal cycle

S = seasonal cycle

T = trends (long-term signal, local effects, ENSO, NAO, Volcanoes, Solar Cycles etc.)

M = microclimate influences (topography, proximity to coastlines, prevailing winds, local environment etc.)







The Non-Climate Bits of Climate

$$X_{(t,l,h)} = XCLIM_{(t,l,h)} + \epsilon_{t,l,h} + \lambda_{t,l,h}$$

X = observation at time t, location l and height h

XCLIM = a climate element at time/location/height

ε = random error at time/place/height

(recording error, instrument error etc.)

λ = systematic error at time/place/height *possibly correlated* (station move, exposure change, instrument change, observing practice change, urbanisation etc.)



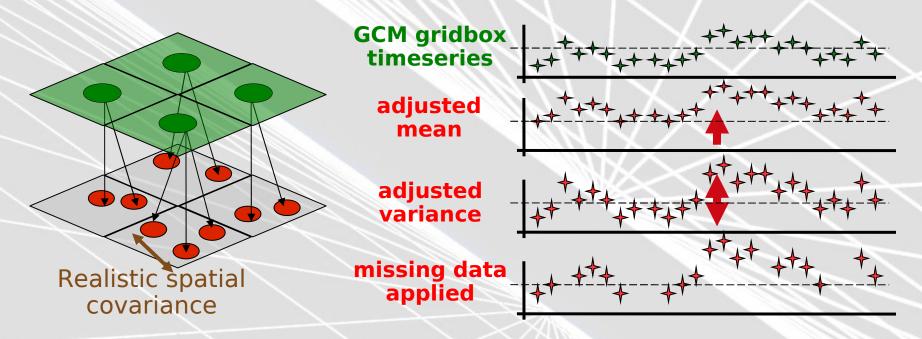


The Concept

'Truth' unknown

Team Creation

$$\mathsf{XTRUTH}_{(t,l,h)} = \mathsf{D}_{t,l,h} + \mathsf{S}_{t,l,h} + \mathsf{T}_{t,l,h} + \mathsf{M}_{t,l,h} + \varepsilon_{t,l,h}$$



Reproduce actual station climatology, variance and interstation relationships

Realistic global station coverage ~60000!

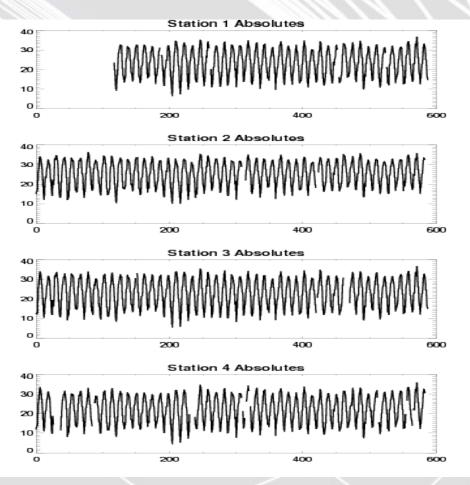
1) Choose a climate model gridbox and create a month anomaly series (subtract month climatology and divide by month standard deviation)

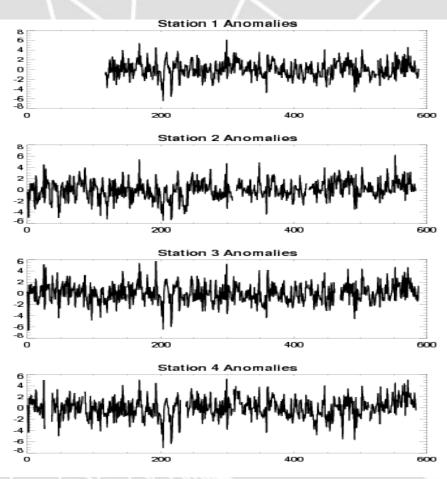
2) Get all observing stations within that gridbox

3) Create station weights by distance/elevation from gridbox centre

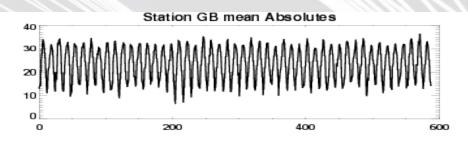
Centre = 1, >150km = 0.5.

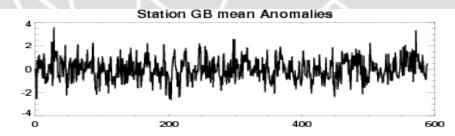
4) Create station climatology, standard deviations, anomalies (subtract month climatology, divide by month standard deviation)



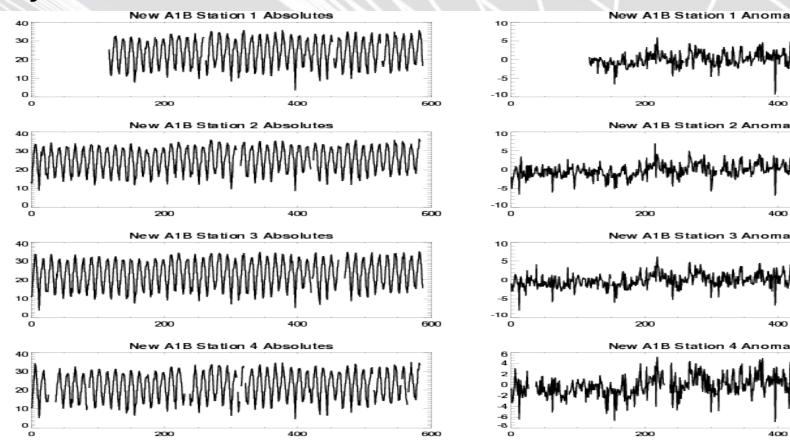


5) Create weighted (using vertical+horizontal distance) gridbox mean from all stations and create anomalies (subtract month climatology, divide by month standard deviation)





6) Create station-GBmean difference series: CAUTION - stations with changepoints may cause problems - these may be introduced into the other station-GBmean series too.



- 7) Test these series to make sure that they are stationary and basically fit an AR(1) model
 - Is it possible to detrend these in a way that is consistent across all series?
 - Infill missing data with climatology or collapse to present data only?
 - treat these series as a matrix [X] n by K:
 n rows for the number of months in the time series
 K columns for the number of stations (4)

$$[X] = \begin{bmatrix} X_{1,1} & X_{1,2} & X_{1,3} & X_{1,4} \\ X_{2,1} & X_{2,2} & X_{2,3} & X_{2,4} \\ & & & \\ X_{n,1} & X_{n,2} & X_{n,3} & X_{n,4} \end{bmatrix}$$

8) Model the multivariate station-GBmean relationship in standardised anomaly space

- do something clever involving a lot of covariance matrices:

 Φ = the autoregressive parameter a K by K matrix - fixed over time

 Z_{+} = the random shock bit

a K by K matrix for each time point?

A distribution based on the variance-covariance matrix such that a random value is plucked for each time point?

 Γ = calculated for lag=0 ($\Gamma(0)$?) and lag=1 ($\Gamma(1)$?)

- this gives a way of simulating values of $X_{1-n,1}$, $X_{1-n,2}$... for example based on some initial starting value (?) governed by an AR(1) model which should hopefully replicate the 'noise' in X but hopefully not incorporate any significant systematic bias (tricky – but hoping the differencing will have reduced this)

9) Create new difference (i.e., station-GBmean) series for each station using the model:

$$\boldsymbol{A}_{_{\boldsymbol{t}}} = \boldsymbol{\varphi}\boldsymbol{A}_{_{\boldsymbol{t}\boldsymbol{\boldsymbol{\cdot}}\boldsymbol{1}}} + \boldsymbol{Z}_{_{\boldsymbol{t}}}$$

- such that

$$[A] = \begin{bmatrix} A_{1,1} & A_{1,2} & A_{1,3} & A_{1,4} \\ A_{2,1} & A_{2,2} & A_{2,3} & A_{2,4} \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & \\ & & & & \\ & & & & \\ & & & & \\ &$$

10) Add the standardised anomalies of the Climate model gridbox to each station difference series in A:

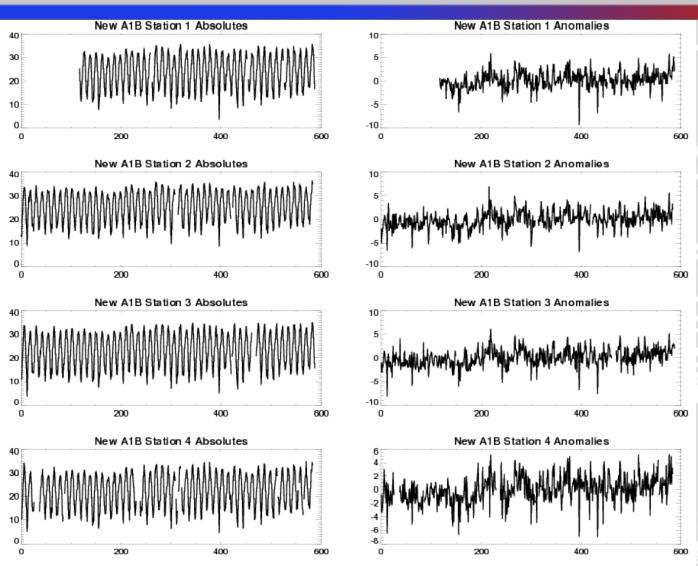
- such that

11) Add back each station's month climatology and multiply by its month standard deviation to product the analog-known-worlds

- may need to add white noise
- mask with actual missing data points from real stations
- CHECK IT DOESN'T CONTAIN ANY CHANGEPOINTS?

This gives 4 analog-known-worlds based on a Climate model background time series using the station microclimate information from the real stations.

Creation: Result?



Same missing data

Same climatological means

Same variance

Similar interstation correlations for a plausible climate scenario over time

No systematic biases